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Simple CPU design and the run-time stack

Where we left off

- We have translated expressions, statements, conditions and loops into TAC
- We stopped at function parameters, call and return
- I'd like to dwell on those for a bit, because their implementation attaches to CPU design specifics

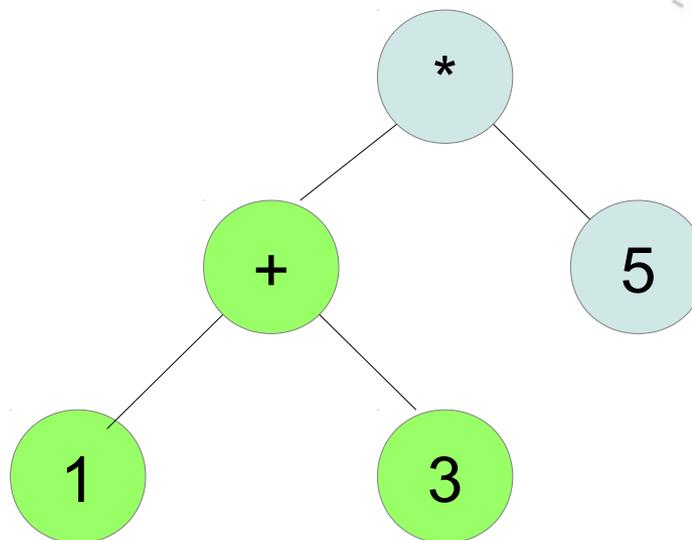


From tree to TAC

$$t1 = 1$$

$$t2 = 3$$

$$t3 = t1 + t2$$



From tree to TAC

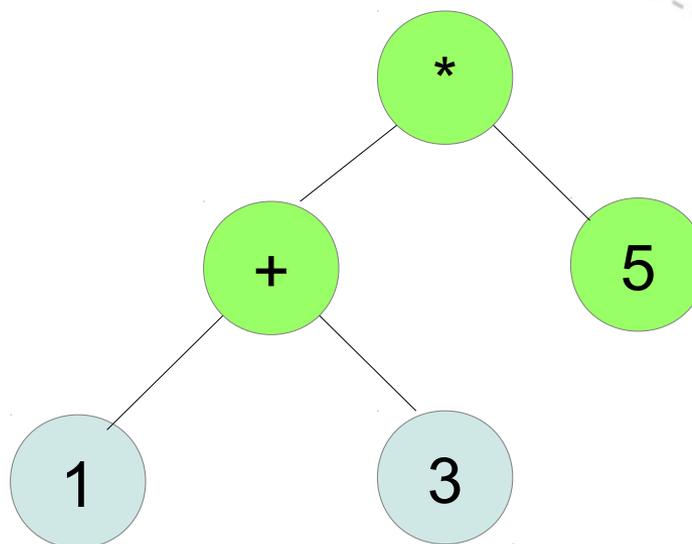
$$t1 = 1$$

$$t2 = 3$$

$$t3 = t1 + t2$$

$$t4 = 5$$

$$t5 = t3 * t4$$



A very simple CPU

- Suppose we have a machine with
 - A register to track its position in the program (**P**rogram **C**ounter)
 - Three slots for numbers (A, B, C)
 - Some memory
 - Operations to load, store, and combine values in registers

PC	A
0	0
B	C
0	0



From TAC to operations

- 1) $t1 = 1$
- 2) $t2 = 3$
- 3) $t3 = t1 + t2$
- 4) $t4 = 5$
- 5) $t5 = t3 * t4$

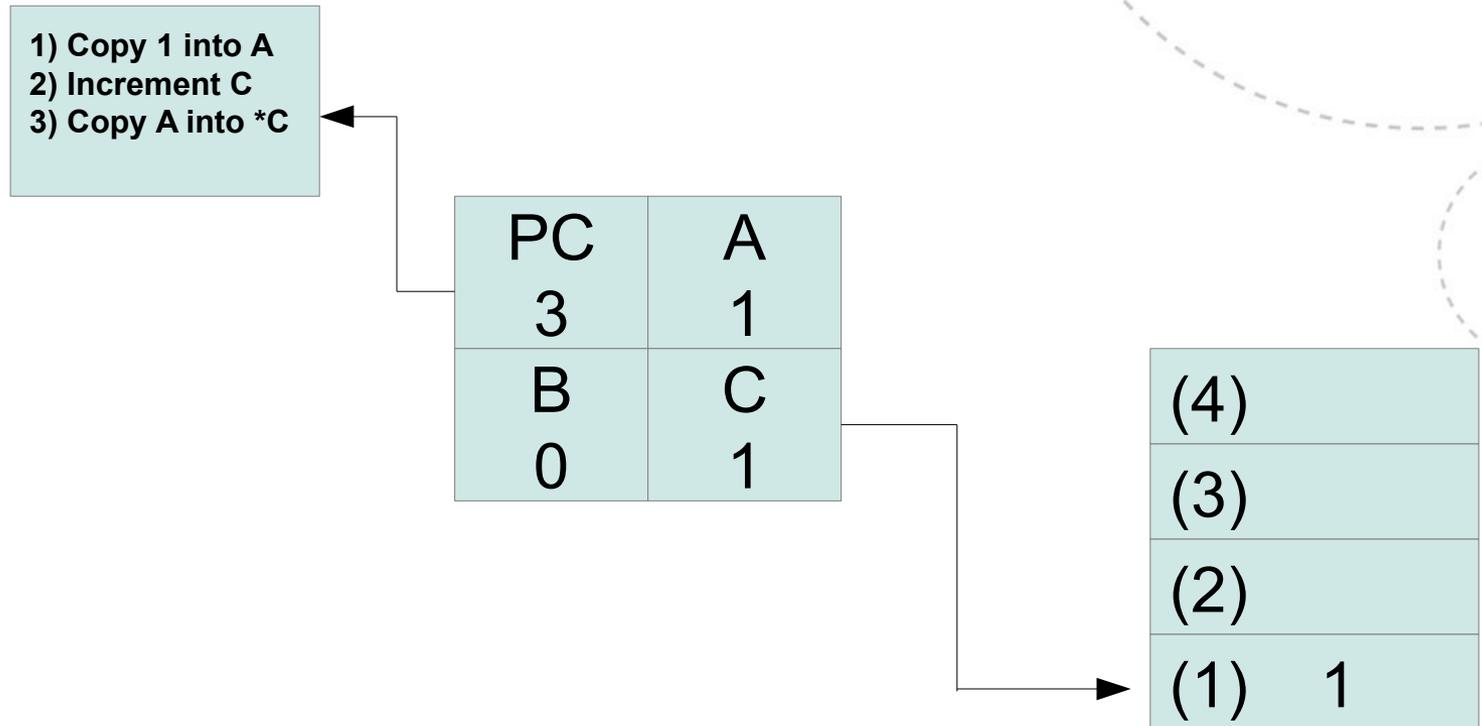
PC	A
1	0
B	C
0	0

(4)
(3)
(2)
(1)



First step on a simple machine

$t1 = 1$
 $t2 = 3$
 $t3 = t1 + t2$
 $t4 = 5$
 $t5 = t3 * t4$



Another step much like it

$t1 = 1$
 $t2 = 3$
 $t3 = t1 + t2$
 $t4 = 5$
 $t5 = t3 * t4$

- 1) Copy 1 into A
- 2) Increment C
- 3) Copy A into *C
- 4) Copy 3 into A
- 5) Increment C
- 6) Copy A into *C

PC	A
6	1
B	C
0	1

(4)	
(3)	
(2)	3
(1)	1



Evaluation of an intermediate result

$t1 = 1$

$t2 = 3$

$t3 = t1 + t2$

$t4 = 5$

$t5 = t3 * t4$

- 1) Copy 1 into A
- 2) Increment C
- 3) Copy A into *C
- 4) Copy 3 into A
- 5) Increment C
- 6) Copy A into *C
- 7) Copy *C into A
- 8) Decrement C
- 9) Copy *C into B
- 10) Decrement C

PC	A
10	3
B	C
1	0

(4)	
(3)	
(2)	3
(1)	1



Evaluation of an intermediate result

$t1 = 1$
 $t2 = 3$
 $t3 = t1 + t2$
 $t4 = 5$
 $t5 = t3 * t4$

- 1) Copy 1 into A
- 2) Increment C
- 3) Copy A into *C
- 4) Copy 3 into A
- 5) Increment C
- 6) Copy A into *C
- 7) Copy *C into A
- 8) Decrement C
- 9) Copy *C into B
- 10) Decrement C
- 11) **A = A + B**
- 12) **Increment C**
- 13) **Copy A into *C**

PC	A
13	4
B	C
1	1

(4)	
(3)	
(2)	3
(1)	4

More of the same

$t1 = 1$
 $t2 = 3$
 $t3 = t1 + t2$
 $t4 = 5$
 $t5 = t3 * t4$

- 1) Copy 1 into A
- 2) Increment C
- 3) Copy A into *C
- 4) Copy 3 into A
- 5) Increment C
- 6) Copy A into *C
- 7) Copy *C into A
- 8) Decrement C
- 9) Copy *C into B
- 10) Decrement C
- 11) $A = A + B$
- 12) Increment C
- 13) Copy A into *C
- 14) Copy 5 into A**
- 15) Increment C**
- 16) Copy A into *C**

PC	A
16	5
B	C
1	2

(4)	
(3)	
(2)	5
(1)	4

The final result

t1 = 1
 t2 = 3
 t3 = t1+t2
 t4 = 5
t5 = t3*t4

- 1) Copy 1 into A
- 2) Increment C
- 3) Copy A into *C
- 4) Copy 3 into A
- 5) Increment C
- 6) Copy A into *C
- 7) Copy *C into A
- 8) Decrement C
- 9) Copy *C into B
- 10) Decrement C
- 11) A = A + B
- 12) Increment C
- 13) Copy A into *C
- 14) Copy 5 into A
- 15) Increment C
- 16) Copy A into *C
- 17) Copy *C into A**
- 18) Decrement C**
- 19) Copy *C into B**
- 20) Decrement C**
- 21) A = A * B
- 22) Increment C
- 23) Copy A into *C

PC	A
20	5
B	C
4	0

(4)	
(3)	
(2)	5
(1)	4

The final result

$t1 = 1$
 $t2 = 3$
 $t3 = t1 + t2$
 $t4 = 5$
 $t5 = t3 * t4$

- 1) Copy 1 into A
- 2) Increment C
- 3) Copy A into *C
- 4) Copy 3 into A
- 5) Increment C
- 6) Copy A into *C
- 7) Copy *C into A
- 8) Decrement C
- 9) Copy *C into B
- 10) Decrement C
- 11) $A = A + B$
- 12) Increment C
- 13) Copy A into *C
- 14) Copy 5 into A
- 15) Increment C
- 16) Copy A into *C
- 17) Copy *C into A
- 18) Decrement C
- 19) Copy *C into B
- 20) Decrement C
- 21) $A = A * B$**
- 22) Increment C**
- 23) Copy A into *C**

PC	A
23	20
B	C
4	1

(4)	
(3)	
(2)	5
(1)	20

Many of those operations were repetitive

- Sequences like

 - Set A to (value)

 - Increment C

 - Put value of a in memory at adr. C

appear whenever (value) needs to be stored away

- Sequences like

 - Set A to memory value at adr. C

 - Decrement C

appear when we need them again



Register C isn't special

- The pattern we used to lay out the operations here could just as well have used A or B to track memory locations, and the other two for operations
- The one we choose behaves like a pointer to the top of a stack, because we manipulate it that way

Stack operation support

- This is such a common thing to do that CPU designers embed support for it into the instruction set
- If we *make* register C special by designating it as the stack-pointer register, it can support instructions like

push 5 (Move reg C “forward” & place 5 where it points)

pop B (Put value from adr. in reg C into B & move C “backward”)

and the program shortens to

push 1

push 3

pop A

pop B

A = A + B

push A

...



Stack machines

- Instruction support doesn't mean that the stack pointer register can't contain whatever you like
 - All it tells us is that the value will change as a side effect of push and pop operations
- Popping values off stack doesn't delete them
 - They will just be overwritten when the stack pointer next comes by there
- The scheme is enough to handle arbitrarily complicated expressions
 - There can be as many temporary values on stack as needed, while we use registers for two at a time

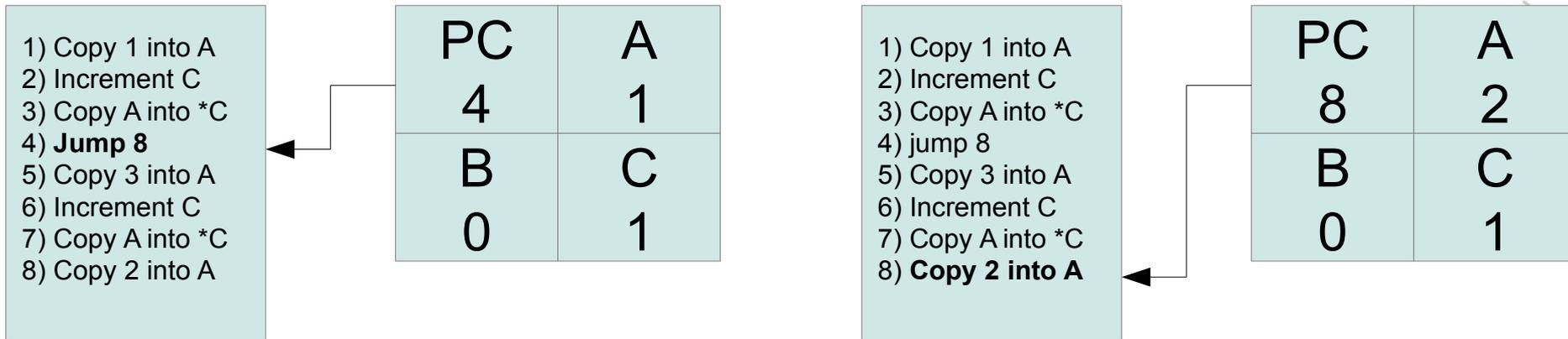
It could be even simpler

- We could get away with
 - one “accumulator” register
 - an implicit stack pointer
 - operations that combine values from the top of the stack into the accumulator
- We could even drop explicit registers altogether, using
 - an implicit stack pointer
 - operations that combine the top two elements
- CPUs like this work, but they result in longer programs with more memory traffic
 - They’re kind of old-fashioned, yet simple to make



Unconditional jumps

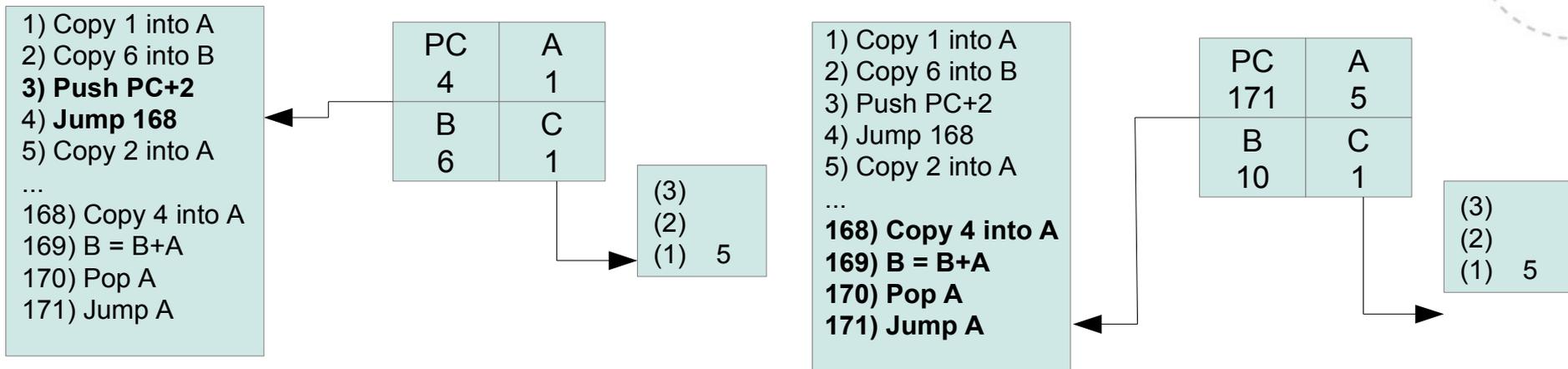
- Jump instructions have a straightforward interpretation in our minimal CPU model
 - they are assignments to the PC register, like so:



(Here, ops 5-7 will never be run)

Simple subroutines

- With memory indexing, we can store the value of PC
- This permits branching off to another part of the program, and coming back again



Jump away...

...do stuff, and
return to where we were



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Those can be operations too

- “Call” translates into
 - Push return address to remember
 - Jump to target
- “Return” translates into
 - Pop address to return to from stack
 - Jump there
- As with “push” and “pop”, call/return are just shorthands for sequences of operations we could also write out explicitly
 - Subroutines make code modular, sections of it can be re-used in several places
 - Subroutines don’t have local context, everything is just a global memory address
 - The GOSUB keyword in many (old) dialects of BASIC works this way



Function call and return

- Translating function calls into this low-level abstraction is a matter of using the stack for two purposes
 - Placing the return location in the program there
 - Placing the values local to the call there
- An *activation record* gives a policy on how to sort these things, so that they can be systematically manipulated and recovered at the appropriate time

IA-32 activation records

- The personal computers of yesteryear had a convention for how to structure stuff on the stack
- It's noticeably cleaner than its present successor, so it merits brief scrutiny
 - Contemporary 64-bit CPUs (Intel and relatives) will still run IA-32 code, they're backwards compatible
 - Contemporary compilers will still generate it, if you tell them to produce 32-bit x86 code (GCC does it with the flag `-m32`)
- We could have used it directly in the practical work, but it grows more contrived each year
 - 16MHz 386/DX: performance monster of 1985
 - I believe in keeping up with progress, even when it's ugly



x86 in 60 seconds

- There's a stack pointer register called ESP
- There's a frame pointer register called EBP
- There are push and pop instructions that manipulate ESP as a side-effect
- There are 2-operand instructions which store the result in one of the operands (move, add, sub, ...)
- There are another few registers
 - We can use EAX and EBX just like A and B from our mini-machine
- There are 'call' and 'ret' operations, as discussed



What's in a function's context?

- Let's take this one, in C:

```
int factorial ( int n ) {  
    int result = n;  
    if ( result > 1 )  
        result *= factorial ( result - 1 );  
    return result;  
}
```

(This is an awful implementation, it's made more to illustrate stack frames than to compute factorials)

Key ingredients

